#### ARITHMETIC PROPERTIES

**ASSOCIATIVE** a(bc) = (ab)c

a + b = b + a and ab = ba**COMMUTATIVE** 

a(b+c) = ab + ac**DISTRIBUTIVE** 

#### ARITHMETIC OPERATIONS EXAMPLES

$$ab + ac = a(b+c)$$

$$a\left(\frac{b}{c}\right) = \frac{ab}{c}$$

$$\frac{a-b}{c-d} = \frac{b-a}{d-c}$$

$$\frac{\left(\frac{a}{b}\right)}{c} = \frac{a}{bc}$$

$$\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$$

$$\frac{a}{\left(\frac{b}{c}\right)} = \frac{ac}{b}$$

$$\frac{ab+ac}{a} = b+c, a \neq 0$$

$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$$

$$\frac{\left(\frac{a}{b}\right)}{\left(\frac{c}{d}\right)} = \frac{ad}{bc}$$

#### QUADRATIC EQUATION

For the equation

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$ax^2 + bx + c = 0$$

#### RADICAL PROPERTIES

 $a, b \ge 0$  for even n

$$\sqrt[n]{a} = a^{\frac{1}{n}}$$

$$\sqrt[m]{\sqrt[n]{a}} = \sqrt[mn]{a}$$

$$\sqrt[n]{ab} = \sqrt[n]{a} \sqrt[n]{b}$$

$$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$$

 $\sqrt[n]{a^n} = a$ , if *n* is odd

 $\sqrt[n]{a^n} = |a|$ , if *n* is even

## LOGARITHM PROPERTIES

if  $y = \log_b x$  then  $b^y = x$ 

 $\log_b b = 1$  and  $\log_b 1 = 0$ 

$$\log_b b^x = x$$

$$b^{\log_b x} = x$$

$$\log_a x = \frac{\log_b x}{\log_b a}$$

$$\log_b(x^r) = r \log_b x$$

$$\log_b(xy) = \log_b x + \log_b y$$

$$\log_b\left(\frac{x}{y}\right) = \log_b x - \log_b y$$

#### **EXPONENT PROPERTIES**

$$a^n a^m = a^{n+m}$$

$$(a^n)^m = a^{nm}$$

$$(ab)^n = a^n b^n$$

$$a^{-n} = \frac{1}{a^n}$$

$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n = \frac{b^n}{a^n}$$

$$\frac{a^n}{a^m} = a^{n-m} = \frac{1}{a^{m-n}}$$

$$a^0 = 1, a \neq 0$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

$$\frac{1}{a^{-n}} = a^n$$

$$a^{\frac{n}{m}} = \left(a^{\frac{1}{m}}\right)^n = (a^n)^{\frac{1}{m}}$$

#### PROPERTIES OF INEQUALITIES

If a < b then a + c < b + c and a - c < b - c

If a < b and c > 0 then ac < bc and a/c < b/c

If a < b and c < 0 then ac > bc and a/c > b/c

#### PROPERTIES OF COMPLEX NUMBERS

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$$\sqrt{-a} = i\sqrt{a}, \qquad a \ge 0$$

$$(a+bi)+(c+di)=\ a+c+(b+d)i$$

$$(a+bi) - (c+di) = a - c + (b-d)i$$

$$(a+bi)(c+di) = ac - bd + (ad+bc)i$$

$$(a+bi)(a-bi) = a^2 + b^2$$

$$|a+bi| = \sqrt{a^2 + b^2}$$

$$\overline{(a+b\iota)}=a-b\iota$$

$$\overline{(a+bi)}(a+bi) = |a+bi|^2$$

$$\frac{1}{(a+bi)} = \frac{(a-bi)}{(a+bi)(a-bi)} = \frac{a-bi}{a^2+b^2}$$

#### COMMON FACTORING EXAMPLES

$$x^2 - a^2 = (x + a)(x - a)$$

$$x^2 + 2ax + a^2 = (x + a)^2$$

$$x^2 - 2ax + a^2 = (x - a)^2$$

$$x^{2} + (a + b)x + ab = (x + a)(x + b)$$

$$x^3 + 3ax^2 + 3a^2x + a^3 = (x + a)^3$$

$$x^3 + a^3 = (x + a)(x^2 - ax + a^2)$$

$$x^3 - a^3 = (x - a)(x^2 + ax + a^2)$$

$$x^{2n} - a^{2n} = (x^n - a^n)(x^n + a^n)$$

$$x^{2n} - a^{2n} = (x^n - a^n)(x^n + a^n)$$

## **ABSOLUTE VALUE**

$$|a| = \begin{cases} a, & \text{if } a \ge 0 \\ -a, & \text{if } a < 0 \end{cases}$$

$$|a| = |-a|$$

$$|a| \ge 0$$

$$|ab| = |a||b|$$

$$\left|\frac{a}{b}\right| = \frac{|a|}{|b|}$$

$$|a+b| \le |a| + |b|$$

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#### COMPLETING THE SQUARE

$$ax^2 + bx + c = a(\dots)^2 + \text{constant}$$

- 1. Divide by the coefficient a.
- 2. Move the constant to the other side.
- 3. Take half of the coefficient b/a, square it and add it to both sides.
- 4. Factor the left side of the equation.
- 5. Use the square root property.
- 6. Solve for x.

# GEOMETRY SHAPES AND SOLIDS

#### SQUARE

$$P = 4s$$

$$A = s^{2}$$

$$S$$

#### **RECTANGLE**

$$P = 2a + 2b$$

$$A = ab$$

$$D$$

#### **CIRCLE**

$$P = 2\pi r$$

$$A = \pi r^2$$

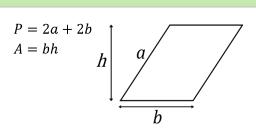
#### **TRIANGLE**

$$P = a + b + c$$

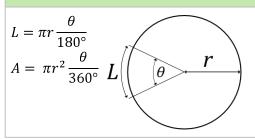
$$A = \frac{1}{2}bh$$

$$h$$

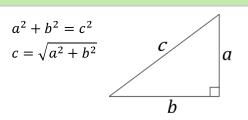
#### PARALLELOGRAM



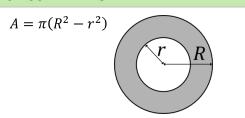
#### CIRCULAR SECTOR



#### **PYTHAGOREAN THEOREM**



#### **CIRCULAR RING**

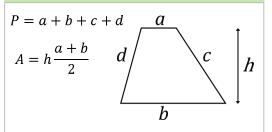


### **SPHERE**

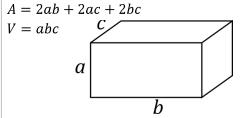




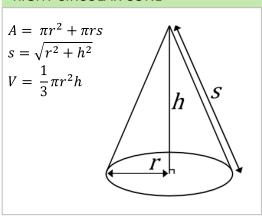
#### **TRAPEZOID**



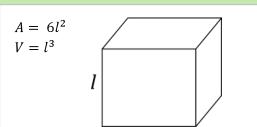
#### **RECTANGULAR BOX**



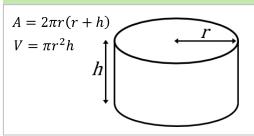
#### RIGHT CIRCULAR CONE



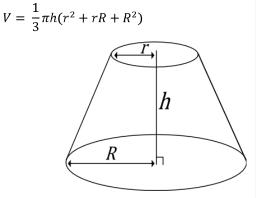
#### CUBE



#### **CYLINDER**



#### FRUSTUM OF A CONE



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